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**bmm**

***Release 1.1***

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**bmm** provides map-matching with uncertainty quantification for both online and offline inference!

Map-matching converts a series of noisy GPS coordinates into a continuous trajectory that is restricted to a graph (i.e. road network) or in the case of **bmm** a collection of continuous trajectories representing multiple plausible routes!

**bmm** is built on top of **osmnx**, an [awesome package for retrieving and processing OpenStreetMap data](#).

The probabilistic model and particle smoothing methodology behind **bmm** can be found on [arXiv](#) and the source code on [GitHub](#).



## 1.1 Functions

`bmm.offline_map_match`(*graph*, *polyline*, *n\_samps*, *timestamps*,  
    *mm\_model*=<*bmm.ExponentialMapMatchingModel* object>, *proposal\_func*=<*function*  
    *optimal\_proposal*>, *d\_refine*=1, *initial\_d\_truncate*=None, *max\_rejections*=20,  
    *ess\_threshold*=1, *store\_norm\_quants*=False, *store\_filter\_particles*=False,  
    *verbose*=True, *\*\*kwargs*)

Runs offline map-matching, i.e. receives a full polyline and returns an equal probability collection of trajectories. Forward-filtering backward-simulation implementation - no fixed-lag approximation needed for offline inference.

### Parameters

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **polyline** (*ndarray*) – series of cartesian coordinates in UTM
- **n\_samps** (*int*) – int number of particles
- **timestamps** (*Union[float, ndarray]*) – seconds either float if all times between observations are the same, or a series of timestamps in seconds/UNIX timestamp
- **mm\_model** (*MapMatchingModel*) – *MapMatchingModel*
- **proposal\_func** (*Callable*) – function to propagate and weight single particle defaults to optimal (discretised) proposal
- **d\_refine** (*int*) – metres, resolution of distance discretisation
- **initial\_d\_truncate** (*Optional[float]*) – distance beyond which to assume zero likelihood probability at time zero defaults to 5 \* *mm\_model.gps\_sd*
- **max\_rejections** (*int*) – number of rejections to attempt before doing full fixed-lag stitching 0 will do full fixed-lag stitching and track *ess\_stitch*
- **ess\_threshold** (*float*) – in [0,1], particle filter resamples if *ess* < *ess\_threshold* \* *n\_samps*
- **store\_norm\_quants** (*bool*) – if True normalisation quantities (including gradient evals) returned in *out\_particles*
- **store\_filter\_particles** (*bool*) – if True filter particles returned in *out\_particles*
- **verbose** (*bool*) – bool whether to print ESS at each iterate
- **kwargs** – optional parameters to pass to proposal i.e. *d\_max*, *d\_refine* or *var* as well as *ess\_threshold* for backward simulation update

**Returns**

MMParticles object

**Return type**

[MMParticles](#)

```
bmm.initiate_particles(graph, first_observation, n_samps,  
                      mm_model=<bmm.ExponentialMapMatchingModel object>, d_refine=1,  
                      d_truncate=None, ess_all=True, filter_store=True)
```

Initiate start of a trajectory by sampling points around the first observation. Note that coordinate system of inputs must be the same, typically a UTM projection (not longitude-latitude!).

**Parameters**

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **mm\_model** (*MapMatchingModel*) – *MapMatchingModel*
- **first\_observation** (*ndarray*) – cartesian coordinate in UTM
- **n\_samps** (*int*) – number of samples to generate
- **d\_refine** (*float*) – metres, resolution of distance discretisation
- **d\_truncate** (*Optional[float]*) – metres, distance beyond which to assume zero likelihood probability defaults to  $5 * \text{mm\_model.gps\_sd}$
- **ess\_all** (*bool*) – if true initiate effective sample size for each particle for each observation otherwise initiate effective sample size only for each observation
- **filter\_store** (*bool*) – whether to initiate storage of filter particles and weights

**Returns**

MMParticles object

**Return type**

[MMParticles](#)

```
bmm.update_particles(graph, particles, new_observation, time_interval,  
                    mm_model=<bmm.ExponentialMapMatchingModel object>, proposal_func=<function  
                    optimal_proposal>, update='BSi', lag=3, max_rejections=20, **kwargs)
```

Updates particle approximation in receipt of new observation

**Parameters**

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **particles** (*MMParticles*) – unweighted particle approximation up to the previous observation time
- **new\_observation** (*ndarray*) – cartesian coordinate in UTM
- **time\_interval** (*float*) – time between last observation and newly received observation
- **mm\_model** (*MapMatchingModel*) – *MapMatchingModel*
- **proposal\_func** (*Callable*) – function to propagate and weight single particle
- **update** (*str*) –
  - ‘PF’ for particle filter fixed-lag update
  - ‘BSi’ for backward simulation fixed-lag updatemust be consistent across updates



- **lag** (*int*) – fixed lag for resampling/stitching
- **max\_rejections** (*int*) – number of rejections to attempt before doing full fixed-lag stitching 0 will do full fixed-lag stitching and track `ess_stitch`
- **kwargs** – optional parameters to pass to proposal i.e. `d_max`, `d_refine` or `var` as well as `ess_threshold` for backward simulation update

**Returns**

MMParticles object

**Return type**

[MMParticles](#)

```
bmm._offline_map_match_fl(graph, polyline, n_samps, timestamps,
                           mm_model=<bmm.ExponentialMapMatchingModel object>,
                           proposal_func=<function optimal_proposal>, update='BSi', lag=3, d_refine=1,
                           initial_d_truncate=None, max_rejections=20, verbose=True, **kwargs)
```

Runs offline map-matching but uses online fixed-lag techniques. Only recommended for simulation purposes.

**Parameters**

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **polyline** (*ndarray*) – series of cartesian coordinates in UTM
- **n\_samps** (*int*) – int number of particles
- **timestamps** (*Union[float, ndarray]*) – seconds, either float if all times between observations are the same, or a series of timestamps in seconds/UNIX timestamp
- **mm\_model** ([MapMatchingModel](#)) – [MapMatchingModel](#)
- **proposal\_func** (*Callable*) – function to propagate and weight single particle defaults to optimal (discretised) proposal
- **update** (*str*) –
  - ‘PF’ for particle filter fixed-lag update
  - ‘BSi’ for backward simulation fixed-lag update
 must be consistent across updates
- **lag** (*int*) – fixed lag for resampling/stitching
- **d\_refine** (*int*) – metres, resolution of distance discretisation
- **initial\_d\_truncate** (*Optional[float]*) – distance beyond which to assume zero likelihood probability at time zero, defaults to  $5 * \text{mm\_model.gps\_sd}$
- **max\_rejections** (*int*) – number of rejections to attempt before doing full fixed-lag stitching, 0 will do full fixed-lag stitching and track `ess_stitch`
- **verbose** (*bool*) – bool whether to print ESS at each iterate
- **kwargs** – optional parameters to pass to proposal i.e. `d_max` or `var` as well as `ess_threshold` for backward simulation update

**Returns**

MMParticles object

**Return type**

[MMParticles](#)

`bmm.sample_route(graph, timestamps, num_obs=None, mm_model=<bmm.ExponentialMapMatchingModel object>, d_refine=1.0, start_position=None, num_inter_cut_off=None)`

Runs offline map-matching. I.e. receives a full polyline and returns an equal probability collection of trajectories. Forward-filtering backward-simulation implementation - no fixed-lag approximation needed for offline inference.

#### Parameters

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **timestamps** (*Union[float, ndarray]*) – seconds either float if all times between observations are the same, or a series of timestamps in seconds/UNIX timestamp
- **num\_obs** (*Optional[int]*) – int length of observed polyline to generate
- **mm\_model** (*MapMatchingModel*) – MapMatchingModel
- **d\_refine** (*float*) – metres, resolution of distance discretisation
- **start\_position** (*Optional[ndarray]*) – optional start position; array (u, v, k, alpha)
- **num\_inter\_cut\_off** (*Optional[int]*) – maximum number of intersections to cross in the time interval

#### Returns

tuple with sampled route (array with same shape as a single MMParticles) and polyline (array with shape (num\_obs, 2))

#### Return type

*Tuple[ndarray, ndarray]*

`bmm.random_positions(graph, n=1)`

Sample random positions on a graph. :param graph: encodes road network, simplified and projected to UTM :param n: int number of positions to sample, default 1 :return: array of positions (u, v, key, alpha) - shape (n, 4)

#### Parameters

- **graph** (*MultiDiGraph*) –
- **n** (*int*) –

#### Return type

*ndarray*

`bmm.offline_em(graph, mm_model, timestamps, polylines, save_path, n_ffbsi=100, n_iter=10, gradient_stepsize_scale=0.001, gradient_stepsize_neg_exp=0.5, **kwargs)`

Run expectation maximisation to optimise parameters of `bmm.MapMatchingModel` object. Updates the hyper-parameters of `mm_model` in place.

#### Parameters

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **mm\_model** (*MapMatchingModel*) – MapMatchingModel - of which parameters will be updated
- **timestamps** (*Union[list, float]*) – seconds, either float if all times between observations are the same, or a series of timestamps in seconds/UNIX timestamp, if timestamps given, must be of matching dimensions to polylines
- **polylines** (*list*) – UTM polylines
- **save\_path** (*str*) – path to save learned parameters
- **n\_ffbsi** (*int*) – number of samples for FFBSi algorithm

- **n\_iter** (*int*) – number of EM iterations
- **gradient\_stepsize\_scale** (*float*) – starting stepsize
- **gradient\_stepsize\_neg\_exp** (*float*) – rate of decay of stepsize, in [0.5, 1]
- **kwargs** – additional arguments for FFBSi

**Returns**

dict of optimised parameters

**bmm.plot**(*graph*, *particles=None*, *polyline=None*, *label\_start\_end=True*, *bgcolor='white'*, *node\_color='grey'*, *node\_size=0*, *edge\_color='lightgrey'*, *edge\_linewidth=3*, *particles\_color='orange'*, *particles\_alpha=None*, *polyline\_color='red'*, *polyline\_s=100*, *polyline\_linewidth=3*, *\*\*kwargs*)

Plots particle approximation of trajectory

**Parameters**

- **graph** – NetworkX MultiDiGraph UTM projection encodes road network e.g. generated using OSMnx
- **particles** – MMParticles object (from inference.particles) particle approximation
- **polyline** – list-like, each element length 2 UTM - metres series of GPS coordinate observations
- **label\_start\_end** – bool whether to label the start and end points of the route
- **bgcolor** – str background colour
- **node\_color** – str node (intersections) colour
- **node\_size** – float size of nodes (intersections)
- **edge\_color** – str colour of edges (roads)
- **edge\_linewidth** – float width of edges (roads)
- **particles\_color** – str colour of routes
- **particles\_alpha** – float in [0, 1] plotting parameter opacity of routes
- **polyline\_color** – str colour of polyline crosses
- **polyline\_s** – str size of polyline crosses
- **polyline\_linewidth** – str linewidth of polyline crosses
- **kwargs** – additional parameters to ox.plot\_graph

**Returns**

fig, ax

**bmm.get\_possible\_routes**(*graph*, *in\_route*, *dist*, *all\_routes=False*, *num\_inter\_cut\_off=inf*)

Given a route so far and maximum distance to travel, calculate and return all possible routes on graph.

**Parameters**

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **in\_route** (*ndarray*) – shape = (\_, 9) columns: t, u, v, k, alpha, x, y, n\_inter, d t: float, time u: int, edge start node v: int, edge end node k: int, edge key alpha: in [0,1], position along edge x: float, metres, cartesian x coordinate y: float, metres, cartesian y coordinate d: metres, distance travelled
- **dist** (*float*) – metres, maximum possible distance to travel

- **all\_routes** (*bool*) – if true return all routes possible  $\leq d$  otherwise return only routes of length  $d$
- **num\_inter\_cut\_off** (*int*) – maximum number of intersections to cross in the time interval

**Returns**

list of arrays each array with shape =  $(\_, 9)$  as in\_route each array describes a possible route

**Return type**

list

**bmm.cartesianise\_path**(*graph, path, t\_column=True, observation\_time\_only=False*)

Converts particle or array of edges and alphas into cartesian (x,y) points.

**Parameters**

- **path** – numpy.ndarray, shape= $(\_, 5+)$  columns - (t), u, v, k, alpha, ...
- **t\_column** – boolean describing if input has a first column for the time variable

**Returns**

numpy.ndarray, shape =  $(\_, 2)$  cartesian points

**bmm.get\_geometry**(*graph, edge*)

Extract geometry of an edge from global graph object. If geometry doesn't exist set to straight line.

**Parameters**

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **edge** (*ndarray*) – length = 3 with elements u, v, k \* u: int, edge start node \* v: int, edge end node \* k: int, edge key

**Returns**

edge geometry

**Return type**

*LineString*

**bmm.discretise\_edge**(*graph, edge, d\_refine*)

Discretises edge to given edge refinement parameter. Returns array of proportions along edge, xy cartesian coordinates and distances along edge

**Parameters**

- **graph** (*MultiDiGraph*) – encodes road network, simplified and projected to UTM
- **edge** (*ndarray*) – list-like, length = 3 with elements u, v, k \* u: int, edge start node \* v: int, edge end node \* k: int, edge key
- **d\_refine** (*float*) – metres, resolution of distance discretisation

**Returns**

shape =  $(\_, 4)$  with columns \* alpha: float in  $(0,1]$ , position along edge \* x: float, metres, cartesian x coordinate \* y: float, metres, cartesian y coordinate \* distance: float, distance from start of edge

**Return type**

*ndarray*

**bmm.observation\_time\_indices**(*times*)

Remove zeros (other than the initial zero) from a series

**Parameters**

**times** (*ndarray*) – series of timestamps

**Returns**

bool array of timestamps that are either non-zero or the first timestamp

**Return type**

*ndarray*

`bmm.observation_time_rows(path)`

Returns rows of path only at observation times (not intersections)

**Parameters**

**path** (*ndarray*) – numpy.ndarray, shape=(\_, 5+) columns - t, u, v, k, alpha, ...

**Returns**

trimmed path numpy.ndarray, shape like path

**Return type**

*ndarray*

`bmm.long_lat_to_utm(points, graph=None)`

Converts a collection of long-lat points to UTM :param points: points to be projected, shape = (N, 2) :param graph: optional graph containing desired crs in graph.graph['crs'] :return: array of projected points

**Parameters**

**points** (*Union[list, ndarray]*) –

**Return type**

*ndarray*

## 1.2 Classes

`class bmm.MMParticles(initial_positions)`

Class to store trajectories from a map-matching algorithm.

In particular, contains the `self.particles` object, which is a list of n arrays each with shape = (\_, 8)

where \_ represents the trajectory length (number of nodes that are either intersection or observation) and columns:

- t: seconds, observation time
- u: int, edge start node
- v: int, edge end node
- k: int, edge key
- alpha: in [0,1], position along edge
- x: float, metres, cartesian x coordinate
- y: float, metres, cartesian y coordinate
- d: float, metres, distance travelled since previous observation time

As well as some useful properties: \* `self.n`: number of particles \* `self.m`: number of observations \* `self.observation_times`: array of observation times \* `self.latest_observation_time`: time of most recently received observation \* `self.route_nodes`: list of length n, each element contains the series of nodes traversed for that particle

Initiate MMParticles storage of trajectories with some start positions as input.

**Parameters**

**initial\_positions** (*List[ndarray]*) – list, length = n\_samps, each element is an array of length 6 with elements

- u: int, edge start node
- v: int, edge end node
- k: int, edge key
- alpha: in [0,1], position along edge
- x: float, metres, cartesian x coordinate
- y: float, metres, cartesian y coordinate

**property latest\_observation\_time: float**

Extracts most recent observation time. :return: time of most recent observation

**property m: int**

Number of observations received. :return: number of observations received

**property observation\_times: ndarray**

Extracts all observation times. :return: array, shape = (m,)

**route\_nodes()**

Returns n series of nodes describing the routes :return: length n list of arrays, shape (\_,)

where \_ represents the trajectory length (number of nodes that are either intersection or observation)

**class bmm.MapMatchingModel**

Class defining the state-space model used for map-matching.

**Transition density (assuming constant time interval)**

$$p(x_t, e_t | x_{t-1}) \propto \gamma(d_t) \exp(-\beta |d_t^{\text{gc}} - d_t|) \mathbb{I}[d_t < d_{\max}],$$

where  $d_t$  is the distance between positions  $x_{t-1}$  and  $x_t$  along the series of edges  $e_{t-1}$ , restricted to the graph/road network.  $d_t^{\text{gc}}$  is the *great circle distance* between  $x_{t-1}$  and  $x_t$ , not restricted to the graph/road network.

The  $\exp(-\beta |d_t^{\text{gc}} - d_t|)$  term penalises non-direct or windy routes where  $\beta$  is a parameter stored in `self.deviation_beta`, yet to be defined.

$d_{\max}$  is defined by `self.d_max` function (metres) and `self.max_speed` parameter (metres per second), defaults to 35.

The  $\gamma(d_t)$  term penalises overly lengthy routes and is yet to be defined.

**Observation density**

$$p(y_t | x_t) = \mathcal{N}(y_t | x_t, \sigma_{\text{GPS}}^2 \mathbb{I}_2),$$

where  $\sigma_{\text{GPS}}$  is the standard deviation (metres) of the GPS noise stored in `self.gps_sd`, yet to be defined. Additional optional `self.likelihood_d_truncate` for truncated Gaussian noise, defaults to inf.

The parameters `self.deviation_beta`, `self.gps_sd` and the distance prior parameters defined in `self.distance_params` and `self.distance_params_bounds` can be tuned using expectation-maximisation with `bmm.offline_em`.

For more details see <https://arxiv.org/abs/2012.04602>.

**d\_max**(*time\_interval*)

Initiates default value of the maximum distance possibly travelled in the time interval. Assumes a maximum possible speed.

**Parameters**

**time\_interval** (*float*) – float seconds time between observations

**Returns**

float defaulted d\_max

**Return type**

float

**deviation\_prior\_evaluate**(*previous\_cart\_coord*, *route\_cart\_coords*, *distances*)

Evaluate deviation prior/transition density Vectorised to handle multiple evaluations at once :param previous\_cart\_coord: shape = (2,) or (\_, 2) cartesian coordinate(s) at previous observation time :param route\_cart\_coords: shape = (\_, 2), cartesian coordinates - positions along road network :param distances: shape = (\_,) route distances between previous\_cart\_coord(s) and route\_cart\_coords :return: deviation prior density evaluation(s)

**Parameters**

- **previous\_cart\_coord** (*ndarray*) –
- **route\_cart\_coords** (*ndarray*) –
- **distances** (*ndarray*) –

**Return type**

*ndarray*

**distance\_prior\_bound**(*time\_interval*)

Extracts bound on the distance component of the prior/transition density :param time\_interval: seconds, time between observations :return: bound on distance prior density

**Parameters**

**time\_interval** (*float*) –

**Return type**

float

**distance\_prior\_evaluate**(*distance*, *time\_interval*)

Evaluate distance prior/transition density Vectorised to handle multiple evaluations at once

**Parameters**

- **distance** (*Union[float, ndarray]*) – metres array if multiple evaluations at once
- **time\_interval** (*Union[float, ndarray]*) – seconds, time between observations

**Returns**

distance prior density evaluation(s)

**Return type**

*Union[float, ndarray]*

**distance\_prior\_gradient**(*distance*, *time\_interval*)

Evaluate gradient of distance prior/transition density in distance\_params Vectorised to handle multiple evaluations at once

**Parameters**

- **distance** (*Union[float, ndarray]*) – metres array if multiple evaluations at once

- **time\_interval** (*Union[float, ndarray]*) – seconds, time between observations

**Returns**

distance prior density evaluation(s)

**Return type**

*Union[float, ndarray]*

**likelihood\_evaluate**(*route\_cart\_coords, observation*)

Evaluate probability of generating observation from cartesian coords Vectorised to evaluate over many cart\_coords for a single observation Isotropic Gaussian with standard dev self.gps\_sd :param route\_cart\_coords: shape = (\_, 2), cartesian coordinates - positions along road network :param observation: shape = (2,) observed GPS cartesian coordinate :return: shape = (\_,) likelihood evaluations

**Parameters**

- **route\_cart\_coords** (*ndarray*) –
- **observation** (*ndarray*) –

**Return type**

*Union[float, ndarray]*

**pos\_distance\_prior\_bound**(*time\_interval*)

Extracts bound on the distance component of the prior/transition density given the distance is > 0 :param time\_interval: seconds, time between observations :return: bound on distance prior density

**Parameters**

**time\_interval** (*float*) –

**Return type**

float

```
class bmm.ExponentialMapMatchingModel(zero_dist_prob_neg_exponent=0.133, lambda_speed=0.068,  
                                       deviation_beta=0.052, gps_sd=5.23)
```

Class defining the state-space model used for map-matching with exponential prior on distance travelled.

**Transition density (assuming constant time interval)**

$$p(x_t, e_t | x_{t-1}) \propto \gamma(d_t) \exp(-\beta |d_t^{\text{gc}} - d_t|) \mathbb{I}[d_t < d_{\max}],$$

where  $d_t$  is the distance between positions  $x_{t-1}$  and  $x_t$  along the series of edges  $e_{t-1}$ , restricted to the graph/road network.  $d_t^{\text{gc}}$  is the *great circle distance* between  $x_{t-1}$  and  $x_t$ , not restricted to the graph/road network.

The  $\exp(-\beta |d_t^{\text{gc}} - d_t|)$  term penalises non-direct or windy routes where  $\beta$  is a parameter stored in `self.deviation_beta` defaults to 0.052.

$d_{\max}$  is defined by `self.d_max` function (metres) and `self.max_speed` parameter (metres per second), defaults to 35.

**The  $\gamma(d_t)$  term**

$$\gamma(d_t) = p^0 \mathbb{I}[d_t = 0] + (1 - p^0) \mathbb{I}[d_t > 0] \lambda \exp(-\lambda d_t / \Delta t),$$

penalises overly lengthy routes, defined as an exponential distribution with probability mass at  $d_t = 0$  to account for traffic, junctions etc.

where  $p^0 = \exp(-r^0 \Delta t)$  with  $\Delta t$  being the time interval between observations. The  $r^0$  parameter is stored in `self.zero_dist_prob_neg_exponent` and defaults to 0.133. Exponential distribution parameter  $\lambda$  is stored in `self.lambda_speed` and defaults to 0.068.



## Observation density

$$p(y_t|x_t) = \mathcal{N}(y_t | x_t, \sigma_{\text{GPS}}^2 \mathbb{I}_2),$$

where  $\sigma_{\text{GPS}}$  is the standard deviation (metres) of the GPS noise stored in `self.gps_sd`, defaults to 5.23. Additional optional `self.likelihood_d_truncate` for truncated Gaussian noise, defaults to `inf`.

The parameters `self.deviation_beta`, `self.gps_sd` as well as the distance prior parameters `self.zero_dist_prob_neg_exponent` and `self.lambda_speed` can be tuned using expectation-maximisation with `bmm.offline_em`.

For more details see <https://arxiv.org/abs/2012.04602>.

### Parameters

- **zero\_dist\_prob\_neg\_exponent** (*float*) – Positive parameter such that stationary probability is  $p^0 = \exp(-r^0 \Delta t)$ , defaults to 0.133.
- **lambda\_speed** (*float*) – Positive parameter of exponential distribution over average speed between observations.
- **deviation\_beta** (*float*) – Positive parameter of exponential distribution over route deviation.
- **gps\_sd** (*float*) – Positive parameter defining standard deviation of GPS noise in metres.

### **distance\_prior\_bound**(*time\_interval*)

Extracts bound on the prior/transition density :param time\_interval: seconds, time between observations  
:return: bound on distance prior density

#### Parameters

**time\_interval** (*float*) –

#### Return type

float

### **distance\_prior\_evaluate**(*distance, time\_interval*)

Evaluate distance prior/transition density Vectorised to handle multiple evaluations at once

#### Parameters

- **distance** (*Union[float, ndarray]*) – metres array if multiple evaluations at once
- **time\_interval** (*Union[float, ndarray]*) – seconds, time between observations

#### Returns

distance prior density evaluation(s)

#### Return type

*Union[float, ndarray]*

### **distance\_prior\_gradient**(*distance, time\_interval*)

Evaluate gradient of distance prior/transition density in `distance_params` Vectorised to handle multiple evaluations at once

#### Parameters

- **distance** (*Union[float, ndarray]*) – metres array if multiple evaluations at once
- **time\_interval** (*Union[float, ndarray]*) – seconds, time between observations

#### Returns

distance prior gradient evaluation(s)

**Return type***Union[float, ndarray]***pos\_distance\_prior\_bound**(*time\_interval*)

Extracts bound on the distance component of the prior/transition density given the distance is > 0 :param time\_interval: seconds, time between observations :return: bound on distance prior density

**Parameters****time\_interval** (*float*) –**Return type***float***zero\_dist\_prob**(*time\_interval*)

Probability of travelling a distance of exactly zero :param time\_interval: time between last observation and newly received observation :return: probability of travelling zero metres in time\_interval

**Parameters****time\_interval** (*Union[float, ndarray]*) –**Return type***Union[float, ndarray]*

## 1.3 Index

## INSTALL

```
pip install bmm
```



## QUICKSTART

Load graph and convert to UTM (Universal Transverse Mercator), a commonly used projection of spherical longitude-latitude coordinates into square x-y coordinates:

```
import numpy as np
import pandas as pd
import osmnx as ox
import json
import bmm

graph = ox.graph_from_place('Porto, Portugal')
graph = ox.project_graph(graph)
```

Beware that downloading graphs using `osmnx` can take a few minutes, especially for large cities.

Load polyline and convert to UTM:

```
data_path = 'simulations/porto/test_route.csv'
polyline_longlat = json.loads(pd.read_csv(data_path)['POLYLINE'][0])
polyline_utm = bmm.long_lat_to_utm(polyline_longlat, graph)
```

### 3.1 Offline map-matching

```
matched_particles = bmm.offline_map_match(graph, polyline=polyline_utm, n_samps=100,
↳ timestamps=15)
```

### 3.2 Online map-matching

Initiate with first observation:

```
matched_particles = bmm.initiate_particles(graph, first_observation=polyline_utm[0], n_
↳ samps=100)
```

Update when new observation comes in

```
matched_particles = bmm.update_particles(graph, matched_particles, new_
↳ observation=polyline_utm[1], time_interval=15)
```



## SANITY CHECK

You can manually test that `bmm` is working sensibly for a given graph by generating synthetic data:

```
graph = ox.graph_from_place('London, UK')
graph = ox.project_graph(graph)
generated_route, generated_polyline = bmm.sample_route(graph, timestamps=15, num_obs=20)
```

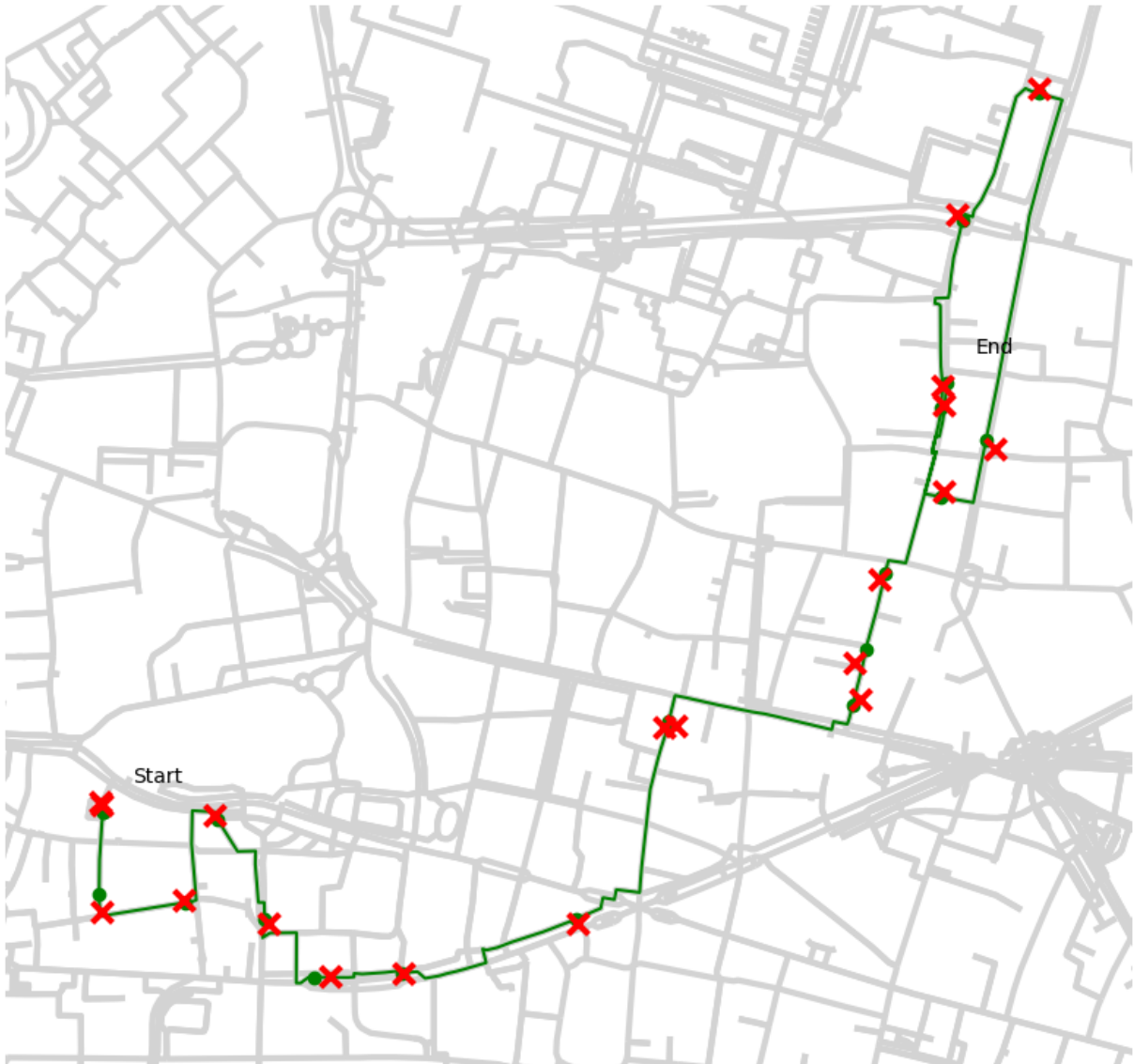
Note that the London graph takes some time (~10mins) to download and for testing on synthetic data it may be worth considering a smaller region (although not so small that the `sample_route` function consistently terminates early due to reaching the edge of the graph).

Run map-matching on the generated polyline:

```
matched_particles = bmm.offline_map_match(graph, generated_polyline, n_samps=100, ↵
↳ timestamps=15)
```

Plot true generated route:

```
bmm.plot(graph, generated_route, generated_polyline, particles_color='green')
```



Plot map-matched particles:

```
bmm.plot(graph, matched_particles, generated_polyline)
```







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